

Report Covid-19 for Spain: April-15

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A dynamical model to predict the Covid-19 in Spain

The model used to predict the Covid-19 evolution in Spain is based on the classical Kermack-Mackendrick models. These models provide a coupled system of three differential equations for the main variables of an epidemic: susceptible, infected and recovered populations.

The model here proposed generalises these models by including constant delays, thus the model continues being a coupled system of differential equations.

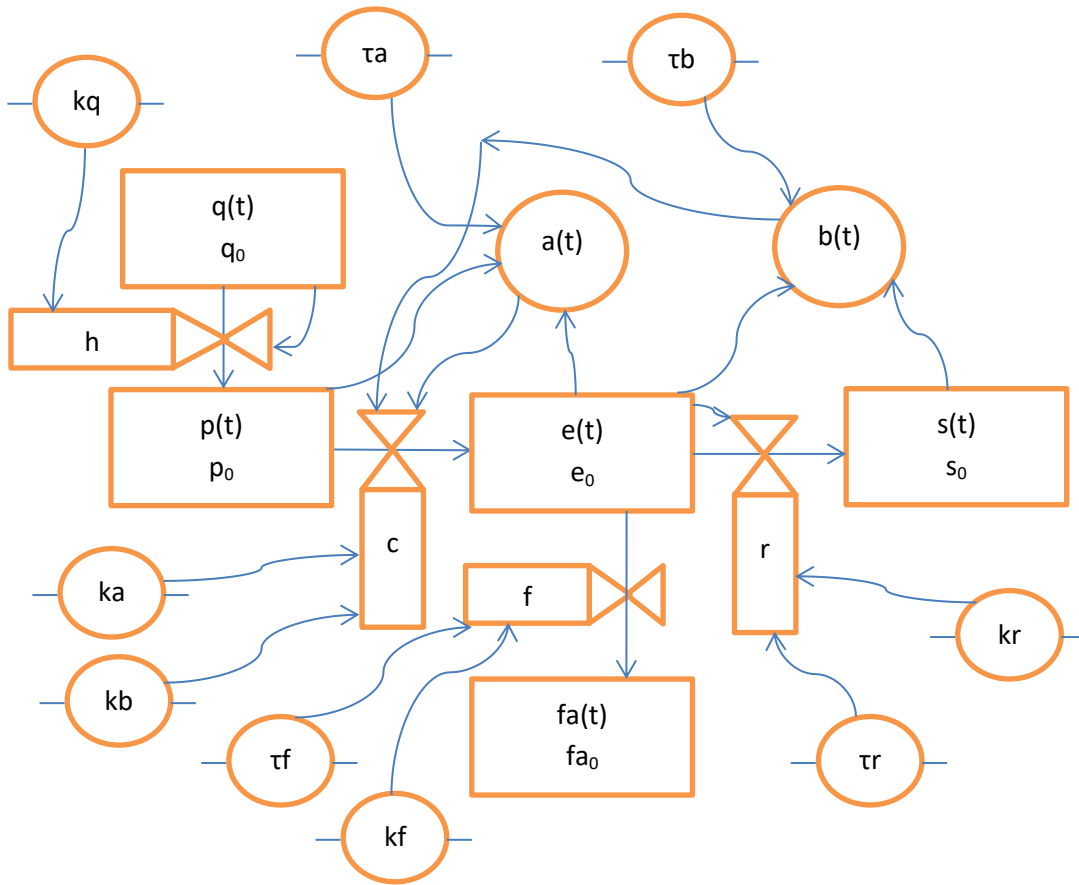
In addition, the Jay W. Forrester methodology, developed in the MIT and generalised in the “Escola d’Investigació Operativa i Sistemes de la ciutat de València” is used. This methodology uses a universal language, represented by the hydrodynamic diagram (Section 1), to build dynamical models of complex systems.

The model presented has input variables or parameters (whose values must be provided) and output variables (Section 2) computed by the system of differential equations (Section 3). To get the parameter values for Spain the model is calibrated by using the experimental data provided by the Spanish Health Ministry (Section 4). We also provide a day to day model update, predicting the infected population values: at short time term for the next three days, and at long time term computing the day and the value of the maximum infected population (Section 5). For any other information, please contact the authors through their electronic mails.

Index

1. Hydrodynamic Diagram.
2. Model variables.
3. Model equations.
4. Model calibration.
5. Short and long time term prediction.
6. Comments.

1. Hydrodynamic Diagram



2. Model variables

2.1. Input variables or parameters:

kq : susceptibility rate

τ_a : continuum susceptible-infected populations interaction delay

τ_b : continuum susceptible-recovered populations interaction delay

ka : susceptible-infected populations interaction rate

kb : susceptible-recovered populations interaction rate

τ_f : continuum infected population deaths delay

kf : infected population deaths rate

τ_r : continuum recovered population delay

kr : recovering population rate

2.2. Output variables (with equation):

$q(t)$: country population (Spain)

$h(t)$: susceptible population flow

$p(t)$: susceptible population
 $c(t)$: infection flow
 $e(t)$: infected population
 $f(t)$: deaths flow
 $fa(t)$: cumulated deaths
 $r(t)$: recovered population flow
 $s(t)$: cumulated recovered population

3. Model equations

$$\frac{dq(t)}{dt} = -h(t)$$

$$h(t) = kq \cdot q(t)$$

$$\frac{dp(t)}{dt} = h(t) - c(t)$$

$$c(t) = ka \cdot a(t) + kb \cdot b(t)$$

$$a(t) = \frac{1}{\tau_a} p(t) \cdot e(t)$$

$$b(t) = \frac{1}{\tau_b} p(t) \cdot s(t)$$

$$\frac{de(t)}{dt} = c(t) - f(t) - r(t)$$

$$ea(t) = e(t) + f(t) + r(t)$$

$$f(t) = \frac{k_f}{\tau_f} e(t)$$

$$r(t) = \frac{k_r}{\tau_r} e(t)$$

$$\frac{ds(t)}{dt} = r(t)$$

$$\frac{dfa(t)}{dt} = f(t)$$

$$\frac{dca(t)}{dt} = c(t)$$

4. Model calibration

The model is calibrated by using the experimental data corresponding to the $ca(t)$, $e(t)$, $fa(t)$ and $s(t)$ variables. They are provided day to day by the Spanish Health Ministry, which can be found in the link:

“<https://www.mscbs.gob.es/profesionales/saludPublica/ccayes/alertasActual/nCov-China/situacionActual.htm>”

The model is implemented in finite differences in SIGEM, developed by Antonio Caselles, and the model calibration is made by the genetic algorithm that SIGEM contains.

First of all, the comparison between the experimental data of the infected and the accumulated infected populations respect to the corresponding theoretical values of the calibrated model is presented. The comparison for today is presented in Figure 1:

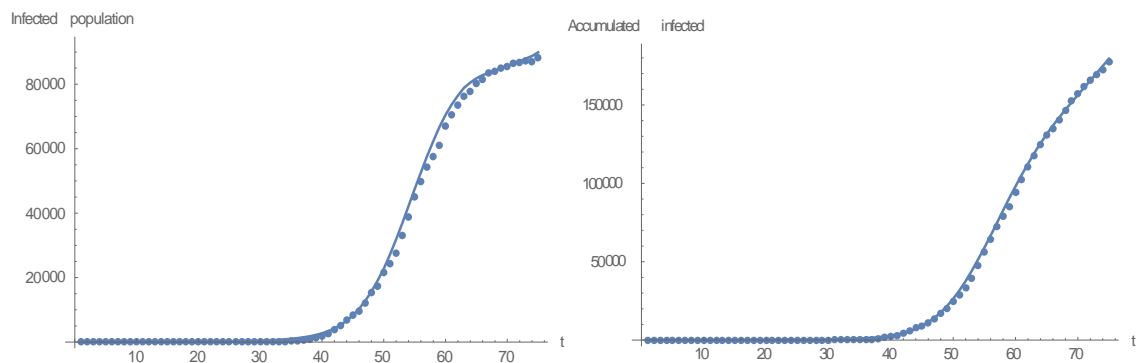


Figure 1: Right: Infected population (dots) and the one predicted by the calibrated model (curve) versus time in days ($R^2=0.999$). **Right:** Accumulated infected population (dots) and the one predicted by the calibrated model (curve) versus time in days ($R^2=0.999$).

Remark: The determination coefficient R^2 varies between 0 and 1. The closer the unit the better the model fits the considered reality.

5. Short and long time term prediction

The prediction objective at short time term is to provide the infected population estimation for the next three days, that is:

Days	Infected population	Accumulated infected
15/04/2020	91212	184182
16/04/2020	92627	188962
17/04/2020	94151	193807

The prediction objective at long time term is to find the infected population peak: the day which the infected population starts to decrease from. See Figure 2, which provides a prediction for 105 days, starting from January 31:

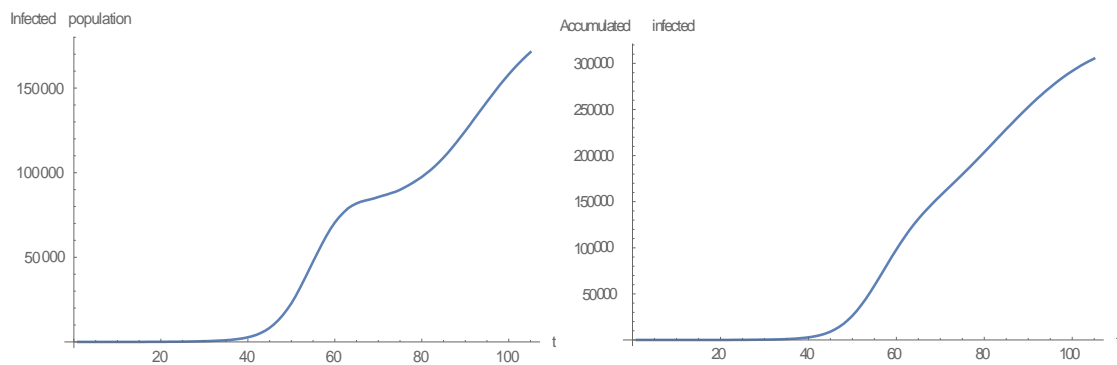


Figure 2: **Left:** Infected population prediction (curve) versus time in days. **Right:** Accumulated infected population prediction (curve) versus time in days (the first day is 2020 January 31).

The collection of data under different conditions, such as tests or asymptomatic infected, breaks the model trends of the last days: Figure 2 shows the **absence of an infected population peak**, and a return to an increasing trend future.

6. Comments

Take into account that the model just provides estimations but not exact values, for both short and long time term predictions. In addition, these predictions can change by considering the incorporation of new data in the model calibration. The model can be improved by:

- (a) Formulating it as a stochastic model, that is, by providing every day predictions with confidence intervals. This improvement would afford more reliability to the model.
- (b) Introducing the political decisions as influences on the parameters. Thus, the model could be a ruling tool for future similar crises.

These improvements will be tried in the collaboration with more scientists, taking into account the present restrictions due to the crisis. For similar comparable approaches see also the following links:

<https://www.systemdynamics.org/covid-19>

<https://covid19.webs.upv.es>

<https://biocomsc.upc.edu/en/covid-19>